

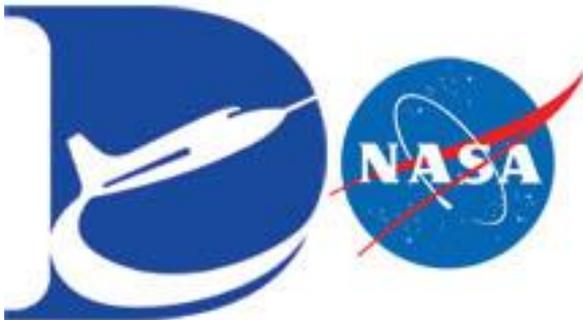
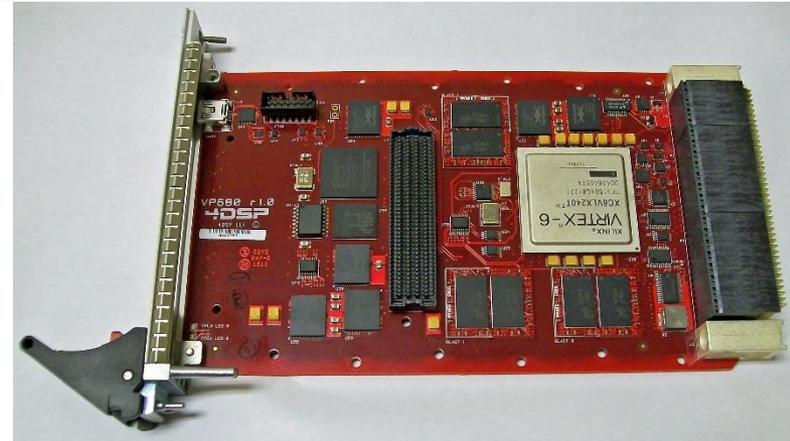
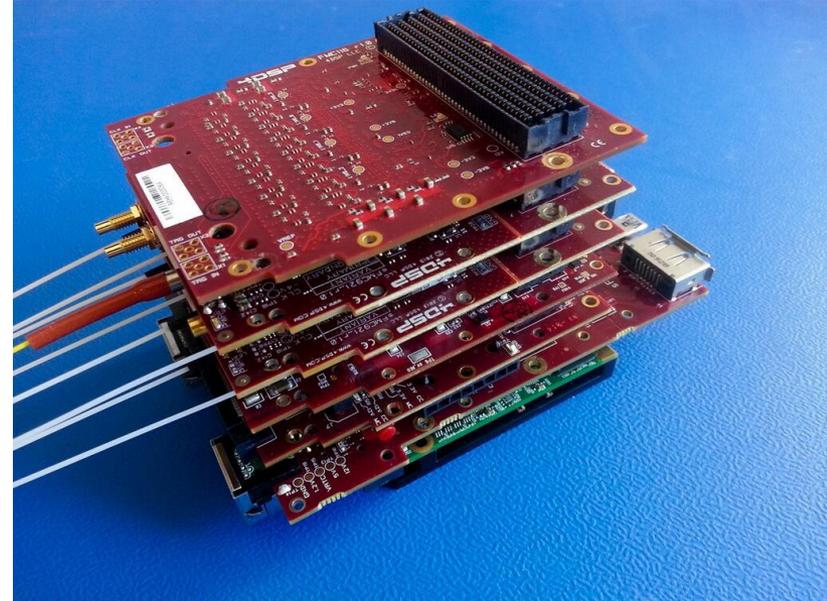
# Shape Sensing using c-OFDR



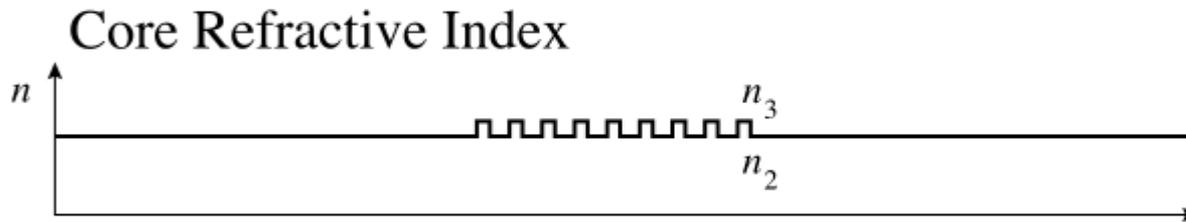
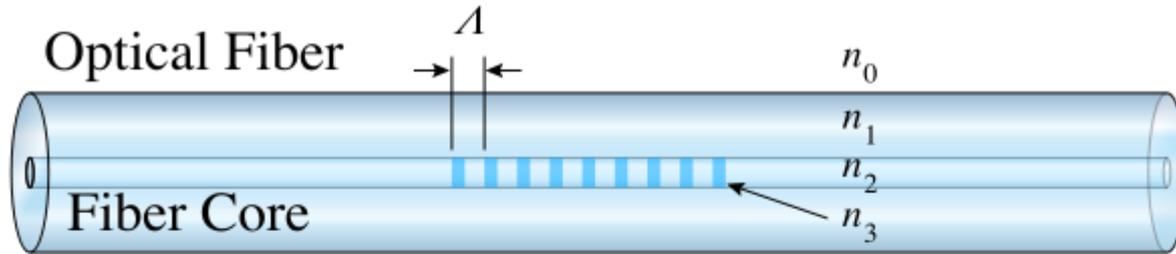
Alex Tongue, 4DSP LLC.

# 4DSP Background

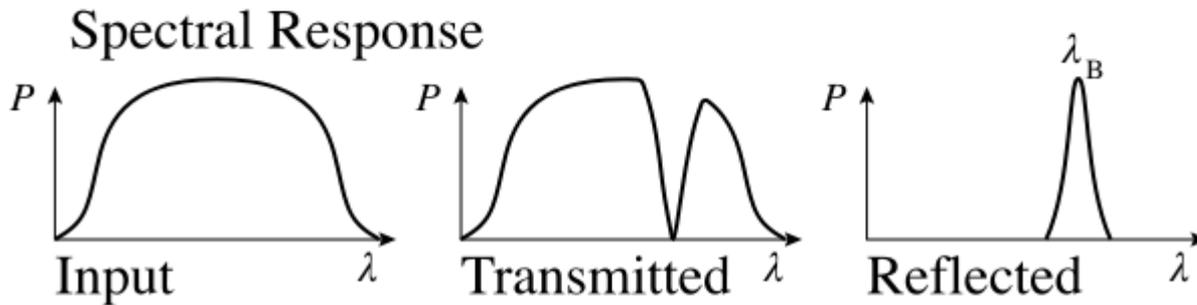
- Founded in 2003
- US and Netherlands offices
- ~25 employees
- NASA fiber optic technology license in 2011
- High speed D/A & A/D hardware and FPGA design



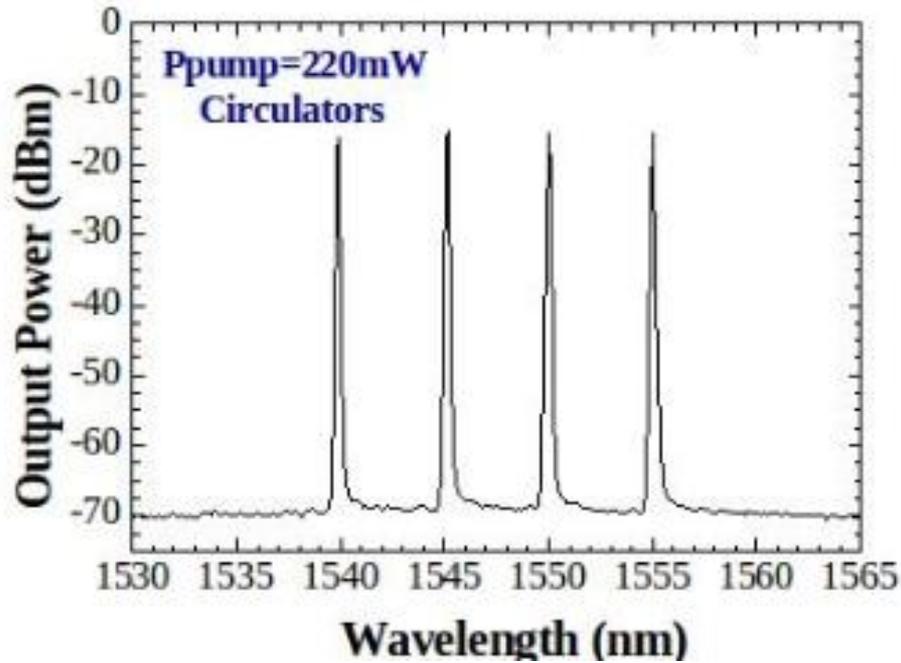
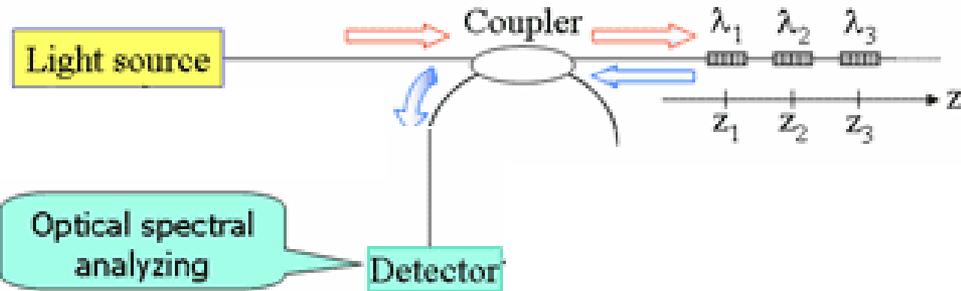
# The Fiber Bragg Grating



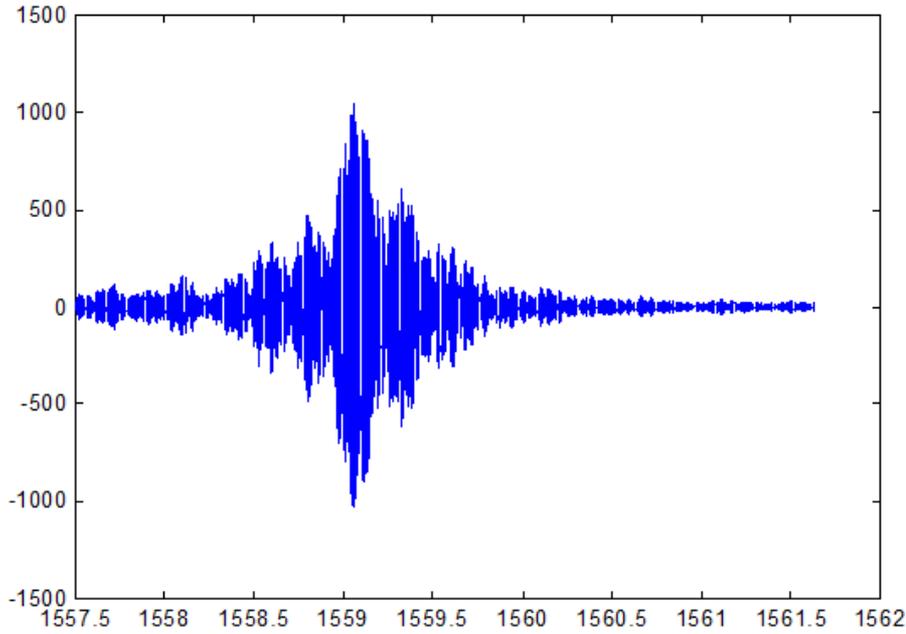
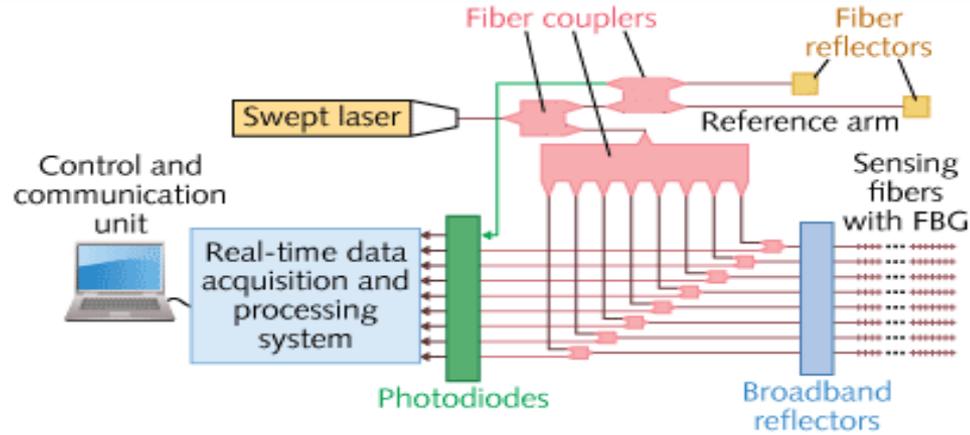
$$\frac{\Delta\lambda}{\lambda} = K\varepsilon$$



# Fiber Interrogation - Traditional



# Fiber Interrogation – c-OFDR

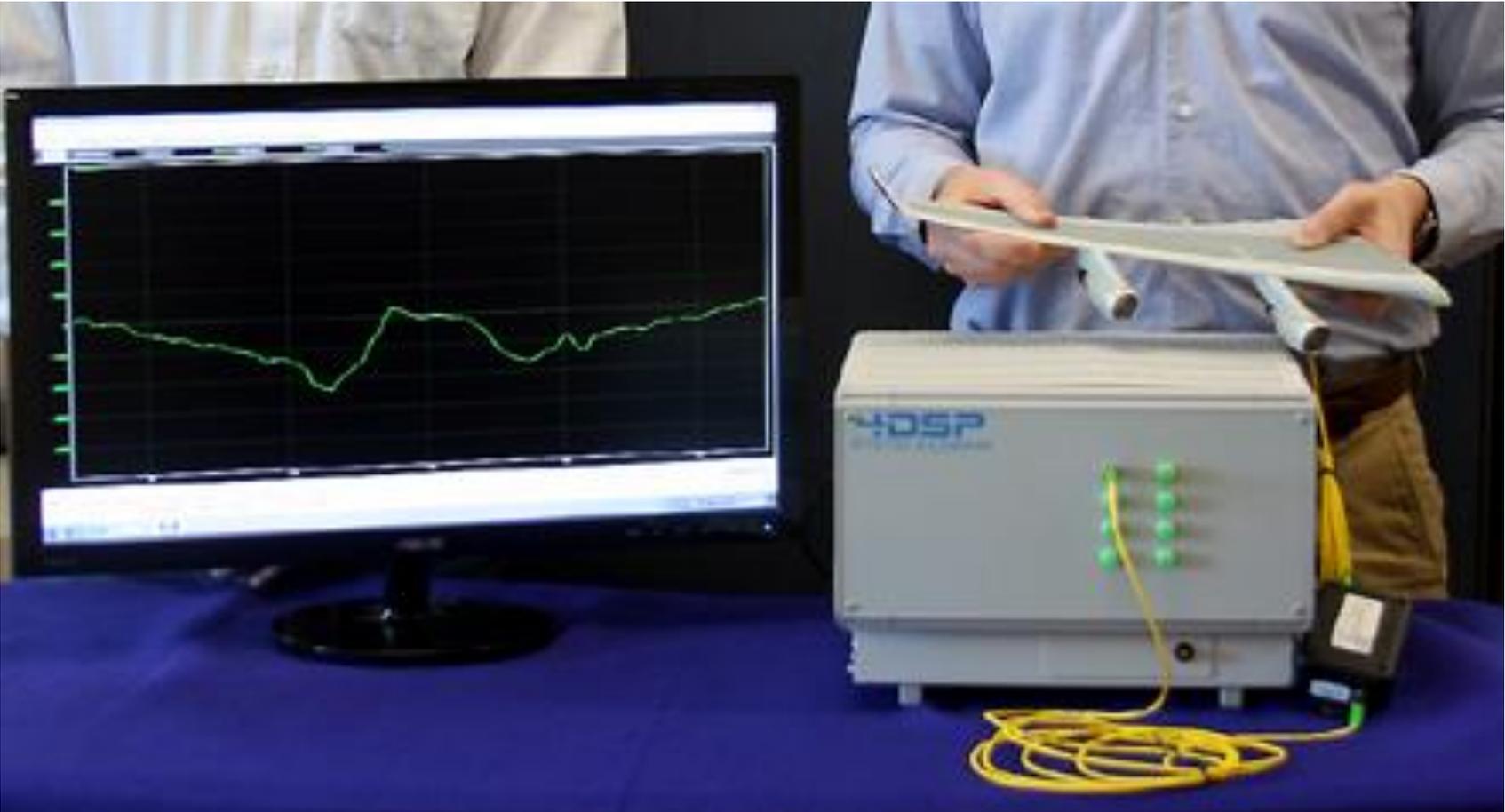


# 4DSP c-OFDR Interrogator



- 8 or 16 Channels
- 2048 sensors per channel
- Up to 100 Hz refresh rate
- User selectable spatial resolution down to 1mm
- Strain, temperature, liquid level, 2- and 3-D shape

# RTS: Distributed Sensing



# 2D Shape Sensing - Motivation



- Helios wing dihedral deflection reached 40 feet during flight
- Exceeded limits and suffered in-flight breakup
- Needed a way to monitor and control deflections during flight and display data to test flight crew

# 2D Shape Sensing - Theory

- Strain  $\longleftrightarrow$  Displacement
- In the case of beams:  $\epsilon_x = -z \frac{d^2w}{dx^2}$
- Thus, cOFDR  $\longrightarrow$   $\epsilon(x)$   $\longrightarrow$   $w(x)$
- Paired with cOFDR, this led to the development of the Dryden Displacement Theory:
  - 2D deflection profile
  - Internal shear and moments
  - Applied loads
  - Only a single fiber optic cable required
  - Bonding of the fiber to the substrate is required

$$y_i = \frac{(\Delta l)^2}{6} \sum_{j=1}^i \frac{1}{c_{j-1}} \left\{ 3(2j-1) - (3j-2) \frac{c_{i-j+1}}{c_{i-j}} \right\} \varepsilon_{i-j} + (3j-2) \varepsilon_{i-j+1} \Big\} + y_0 + i \Delta l \tan \theta_0$$

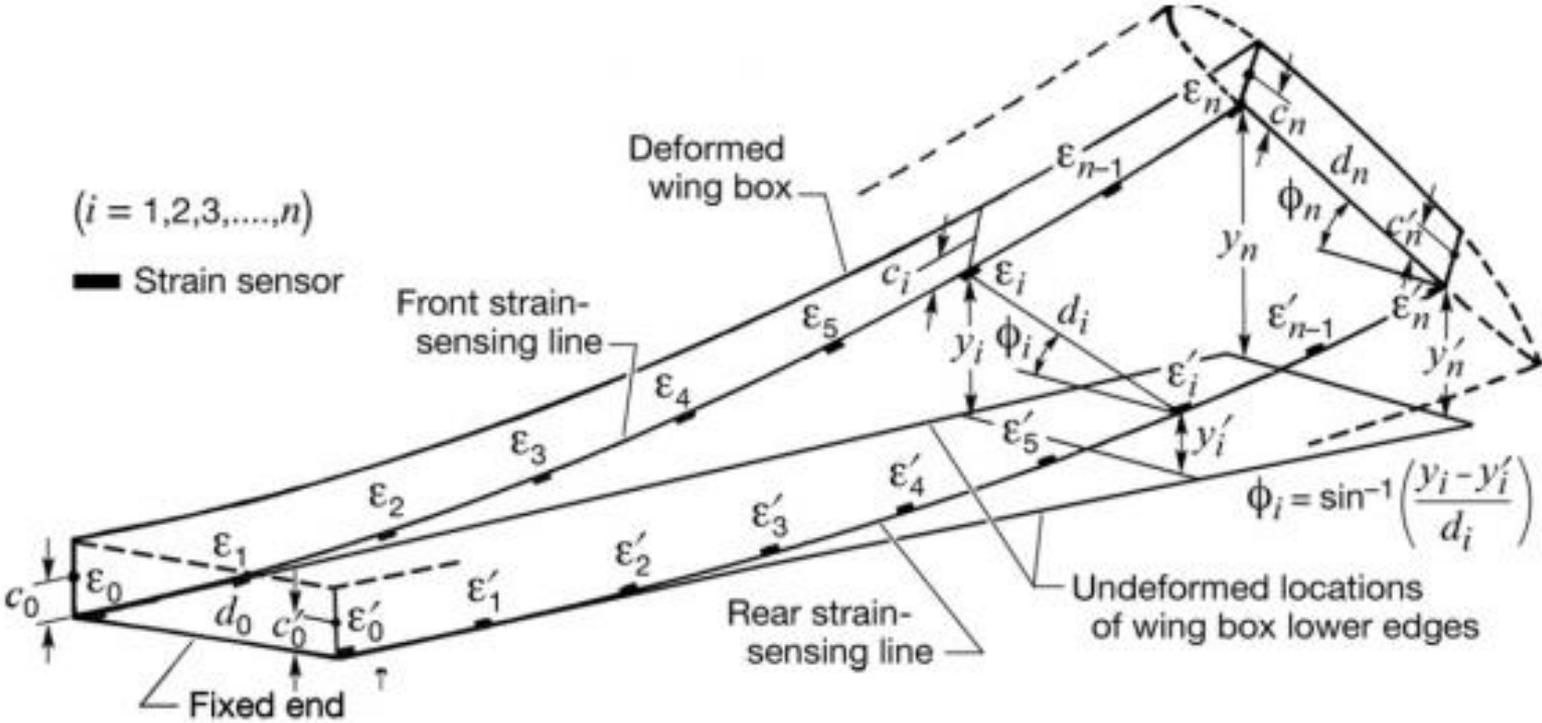
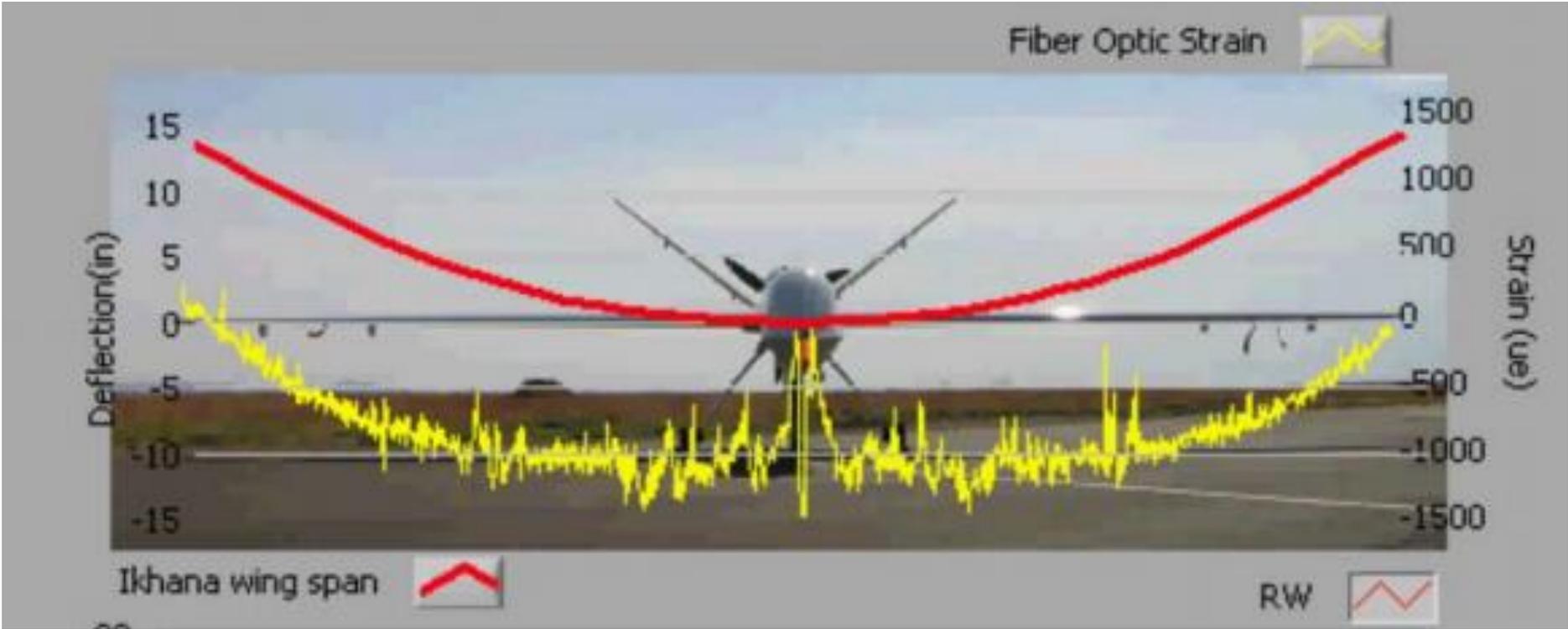
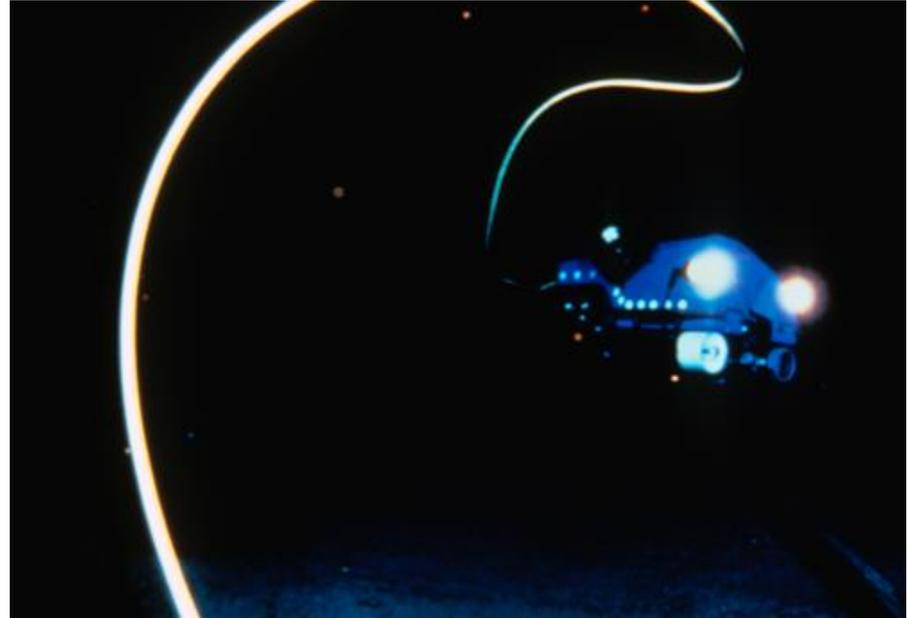
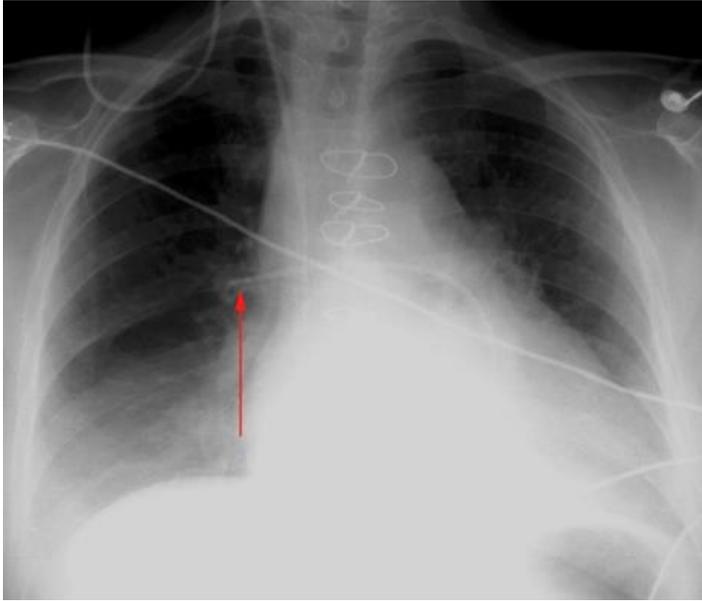


Figure 5-2: Tapered Wing Box Instrumented with Two-Line Strain-Sensing System.

# 2D Shape Sensing - Application



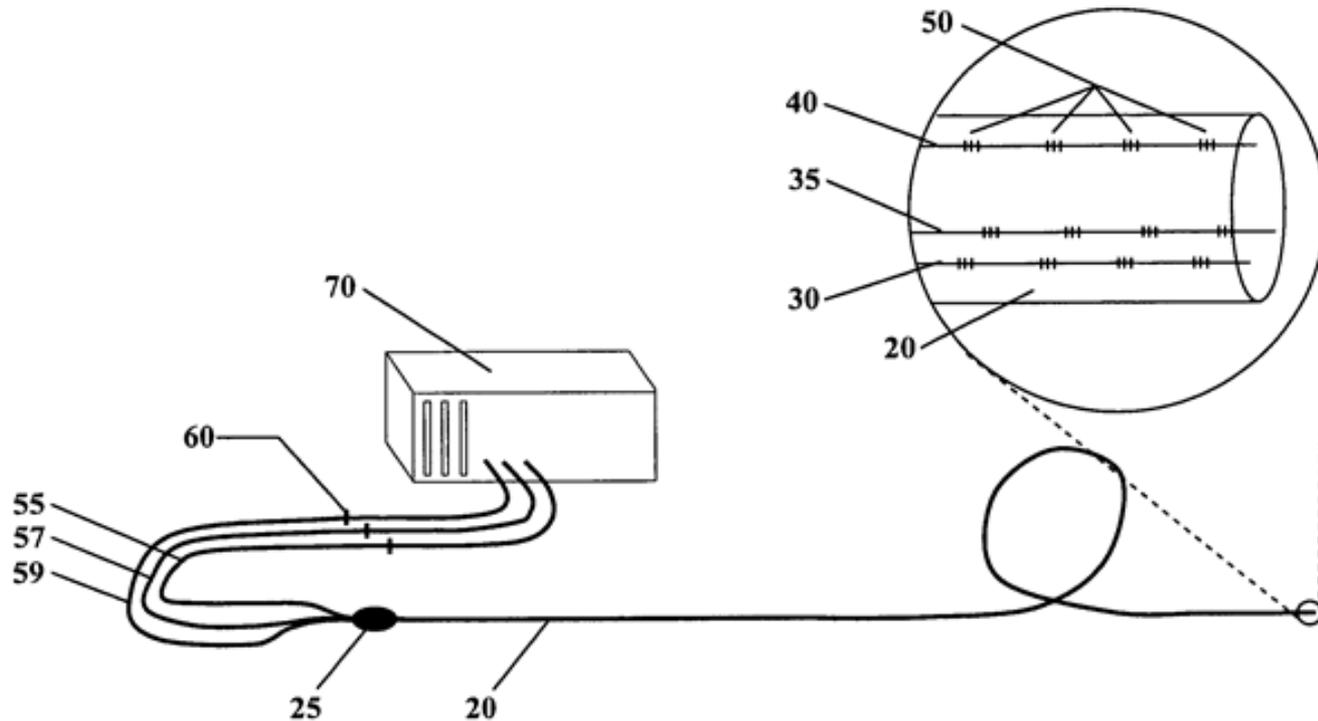
# 3D Shape Sensing - Motivation



- Many other structures may benefit from knowledge of deflection shapes which do not remain in a 2D plane
- Many cabled applications traditionally only track the end location
  - Borescopes
  - Submersible vehicles
- Tracking medical devices often requires additional foreign material and radiation

# 3D Shape Sensing - Theory

- Based on the same strain-displacement principle as the 2D case
- Requires curvature in multiple directions  must use multiple fibers
- Fibers are brought together with a constant cross-sectional geometry
- Connected to the system via a fan-out and three individual connectors



# 3D Shape Sensing - Theory

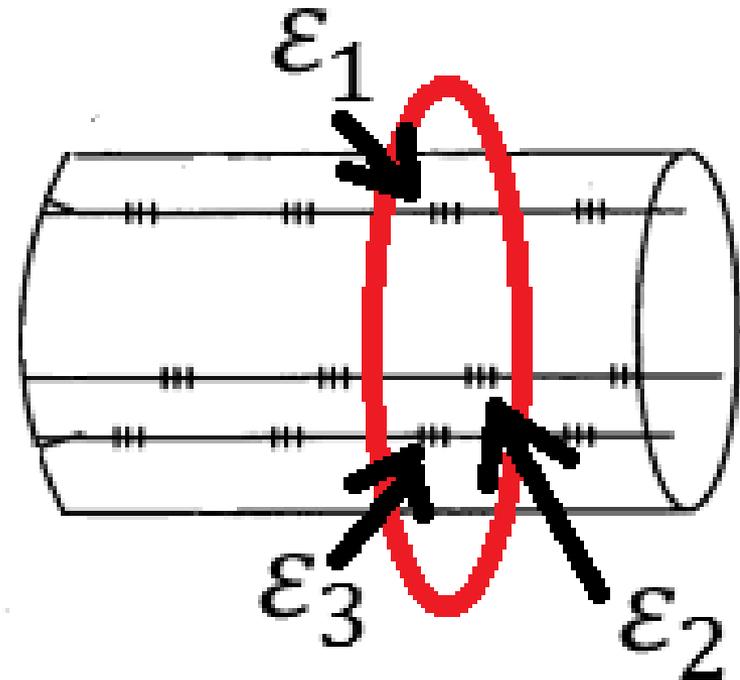
Differential strains are obtained at each sensor “triad”:

$$\Delta \varepsilon_{12} = \varepsilon_1 - \varepsilon_2$$

$$\Delta \varepsilon_{23} = \varepsilon_2 - \varepsilon_3$$

$$\Delta \varepsilon_{31} = \varepsilon_3 - \varepsilon_1$$

Through known geometry, strain-displacement relations, and mathematical descriptions of a curve:



$$\left. \begin{matrix} \Delta \varepsilon_{12} \\ \Delta \varepsilon_{23} \\ \Delta \varepsilon_{31} \end{matrix} \right\} \longrightarrow \left. \begin{matrix} \Delta k_{12} \\ \Delta k_{23} \\ \Delta k_{31} \end{matrix} \right\} \longrightarrow \overline{r(s)}$$

This method yields a sensor which is insensitive to both axial elongation and temperature

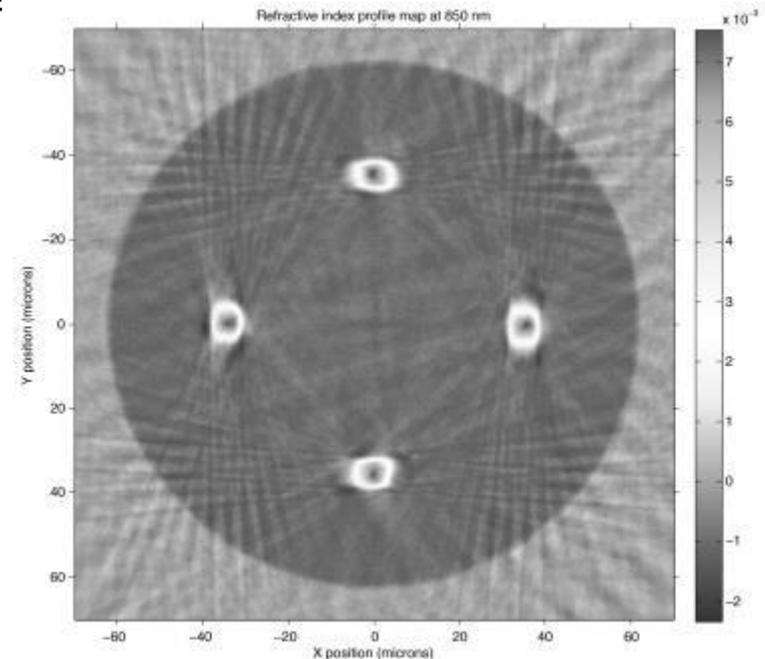
# 3D Shape Sensing – Current and Future

## Current:

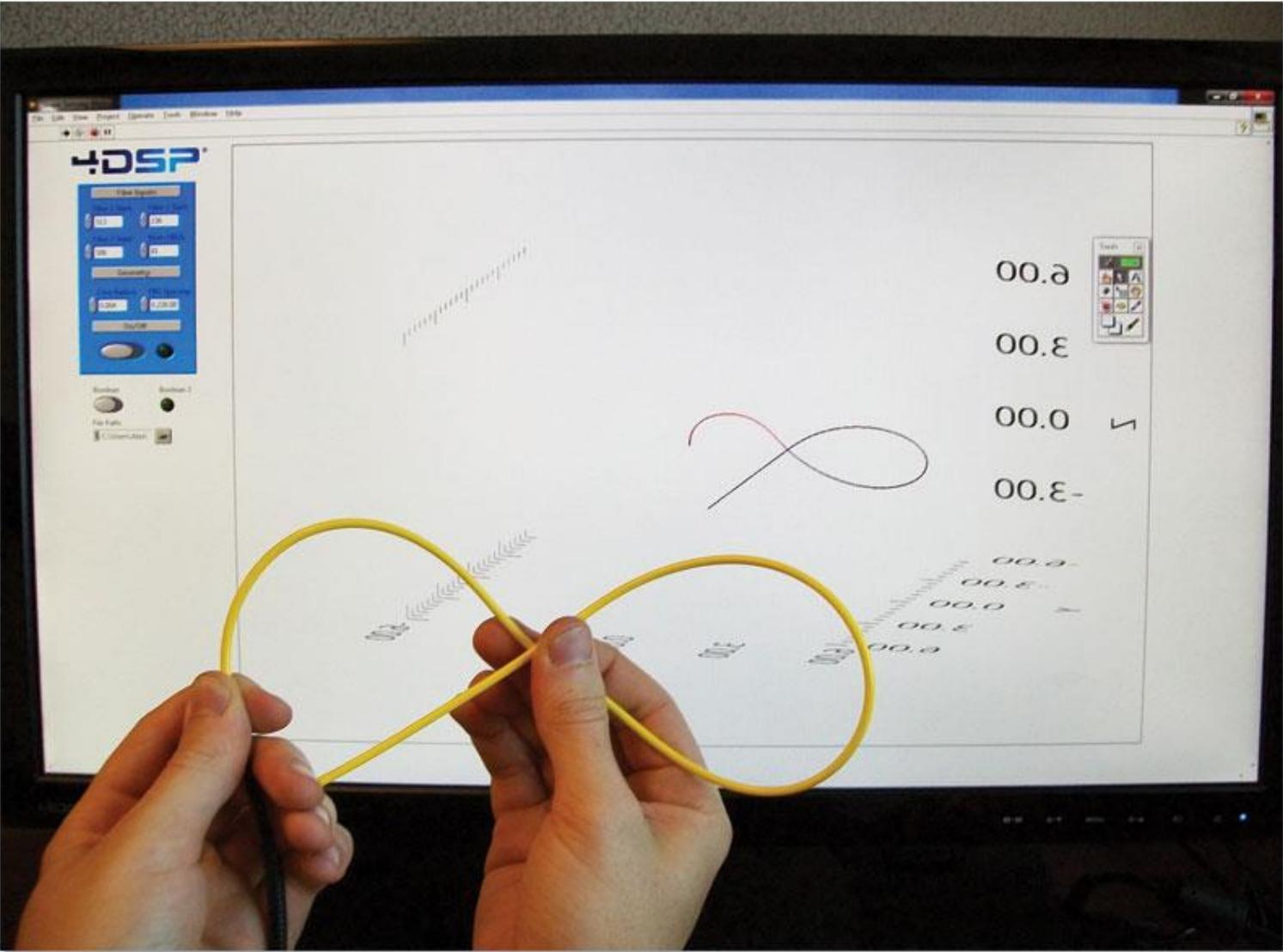
- Sensor integration is currently done by hand and automated production is under development
- Despite being handmade, an initial study for the medical industry yielded positive accuracy and repeatability results
  - 2D testing due to nonuniform cross section
  - Accuracy: 1-3% of arc length
  - Repeatability at end of sensor: <1% of total length
- Lengths of up to 100 m per sensor
- Sensor diameter down to 500 microns

## Future:

- Working with fiber provider (FBGS) on a multicore fiber
- Accuracy <1%
- Twist mitigation
- Sensor diameter down to 330 microns



# 3D Shape Sensing - Output



# 3D Shape Sensing – Output



Thank You  
Questions?

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