



MATH AND SCIENCE @ WORK

AP* PHYSICS Educator Edition



LUNAR SURFACE INSTRUMENTATION

Instructional Objectives

Students will

- add, subtract, and resolve displacement and velocity vectors to determine components of a vector along two specified, mutually perpendicular axes; and
- determine the net displacement of a particle or the location of a particle relative to another.

Degree of Difficulty

For the average AP Physics student, this problem is at a moderate level of difficulty. The problem is a straightforward application of vector concepts.

Class Time Required

This problem requires 40-50 minutes.

- Introduction: 5-10 minutes
 - Read and discuss the background section with the class before students work on the problem. This background is identical to *Training for a New Spacecraft: Moment of Inertia*.
- Student Work Time: 30 minutes
- Post Discussion: 5-10 minutes

Background

This problem is part of a series of problems that apply math and science principles to human space exploration at NASA.

Exploration provides the foundation of our knowledge, technology, resources, and inspiration. It seeks answers to fundamental questions about our existence, responds to recent discoveries and puts in place revolutionary techniques and capabilities to inspire our nation, the world, and the next generation. Through NASA, we touch the unknown, we learn and we understand. As we take our first steps toward sustaining a human presence in the solar system, we can look forward to far-off visions of the past becoming realities of the future.

Grade Level
11-12

Key Topic
Vector Addition

Degree of Difficulty
Moderate

Teacher Prep Time
5 minutes

Problem Duration
40-50 minutes

Technology
Graphing Calculator

Materials
Student Edition including:
- Background handout
- Problem worksheet

Learning Objectives for AP Physics
Newtonian Mechanics:
-Kinematics

NSES
Science Standards
- Science and Technology
- History and Nature of Science

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Outpost concepts are now being designed and studied by engineers, scientists, and sociologists to facilitate long-duration human missions to the surface of the Moon or other planetary bodies (Figure 1). Such outposts will include habitat modules, laboratory modules, power systems, transportation, life support systems, protection from the environment, communications for planetary surface operations, and communications back to Earth.

During past and current space missions, astronaut activity outside of the vehicle (e.g. space shuttle) is referred to as an extravehicular activity, or EVA. In a similar way, extrahabitat activities, or EHA, will be performed during a mission to accomplish exploration work. One EHA may be to place environmental sensors and instruments within the proximity of an outpost (Figure 2).



Figure 1: Habitat, airlock, and vehicles (NASA concept)



Figure 2: Astronaut services a surface instrument (NASA concept)

Such instruments may measure the radiation received from solar flares or characterize micrometeorites impacting the surface. Telescopes may also be set up for observations of Earth, other planets, and stars.

Learning Objectives for AP Physics

Newtonian Mechanics

- Kinematics
 - Vectors, coordinate systems
 - Motions in two dimensions

NSES Science Standards

Science and Technology

- Abilities of technological design

History and Nature of Science

- Science as a Human Endeavour

Problem and Solution Key (One Approach)

An astronaut services three instruments on the relatively flat lunar surface around an equatorial lunar outpost. She starts at the lunar habitat airlock and walks 180 meters southwest to replace the sample cell in the first instrument. She then walks 140 meters due north to add a lens to a second instrument. She finishes the task by walking 100 meters 30 degrees north of east where she resets the pointing of a third instrument. The astronaut walks directly back to the same habitat airlock and reenters the



habitat module. Using a Cartesian coordinate system with the x-axis pointed east and y-axis pointed north, determine the following information for her EHA. Round all answers to one decimal place.

- A. Determine the astronaut’s displacement vector (distance and direction) from the airlock when she is standing at each instrument. Include a sketch of the path taken by the astronaut.

Step 1: Sketch the path taken by the astronaut.

Place the coordinate system origin at the airlock door.

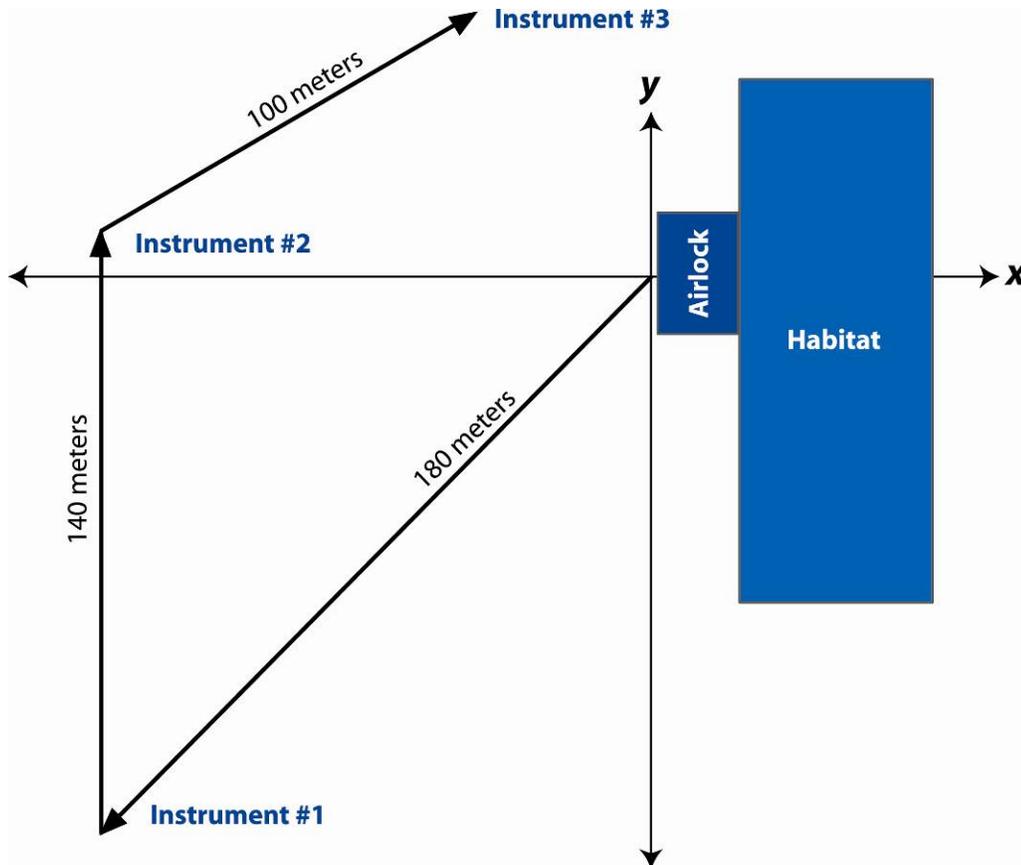


Figure 3: Locations of the lunar surface instruments

Step 2: Determine the (x,y) components of each leg of the trip.

First Leg:

$$x = 180 \cos(225^\circ) = -127.3 \text{ m}$$

$$y = 180 \sin(225^\circ) = -127.3 \text{ m}$$

Second Leg:

$$x = 140 \cos(90^\circ) = 0.0 \text{ m}$$

$$y = 140 \sin(90^\circ) = 140.0 \text{ m}$$



Third Leg:

$$x = 100 \cos(30^\circ) = 86.6 \text{ m}$$

$$y = 100 \sin(30^\circ) = 50.0 \text{ m}$$

Step 3: Determine the (x,y) position of each instrument.

Add successive legs of the trip as vector components.

First leg from the origin to instrument #1:

$$x = 0.0 \text{ m} + (-127.3 \text{ m}) = -127.3 \text{ m}$$

$$y = 0.0 \text{ m} + (-127.3 \text{ m}) = -127.3 \text{ m}$$

Instrument #1 location: (-127.3, -127.3) m

Second leg from instrument #1 to instrument #2:

$$x = -127.3 \text{ m} + 0.0 \text{ m} = -127.3 \text{ m}$$

$$y = -127.3 \text{ m} + 140.0 \text{ m} = 12.7 \text{ m}$$

Instrument #2 location: (-127.3, 12.7) m

Third leg from instrument #2 to instrument #3:

$$x = -127.3 \text{ m} + 86.6 \text{ m} = -40.7 \text{ m}$$

$$y = 12.7 \text{ m} + 50.0 \text{ m} = 62.7 \text{ m}$$

Instrument #3 location: (-40.7, 62.7) m

- B. Determine her displacement (using unit-vector notation) from the airlock when she is standing at each instrument.

Since the three vectors are from the origin to the three instruments, convert the position (x,y) values to vector notation using unit vectors.

$$\text{Instrument \#1: } (-127.3i - 127.3j) \text{ m}$$

$$\text{Instrument \#2: } (-127.3i + 12.7j) \text{ m}$$

$$\text{Instrument \#3: } (-40.7i + 62.7j) \text{ m}$$

- C. Determine the astronaut's displacement from the first instrument and the third instrument.

Step 1: Find the distance between instruments #1 and #3 using the distance formula.

$$d = \sqrt{(y_3 - y_1)^2 + (x_3 - x_1)^2}$$

$$d = \sqrt{(62.7 - (-127.3))^2 + ((-40.7) - (-127.3))^2}$$

$$d = 208.8 \text{ m}$$



Step 2: Find the angle between instruments #1 and #3 using the inverse tangent function.

$$\angle \theta = \tan^{-1} \left(\frac{x_3 - x_1}{y_3 - y_1} \right)$$

$$\angle \theta = \tan^{-1} \left(\frac{-40.7 - (-127.3)}{62.7 - (-127.3)} \right) = 24.5^\circ$$

Instrument #3 is 208.8 m and 24.5° east of north from instrument #1.

D. Determine the distance she walked from the third instrument to the habitat airlock.

$$d = \sqrt{(y_0 - y_3)^2 + (x_0 - x_3)^2}$$

$$d = \sqrt{(0 - 62.7)^2 + (0 - (-40.7))^2}$$

$$d = 74.8 \text{ m}$$

E. Determine the total distance she traveled on her EHA.

First Leg: 180.0 m

Second Leg: 140.0 m

Third Leg: 100.0 m

Fourth Leg: 74.8 m

Sum of the four individual leg lengths.

$$d = 180.0 + 140.0 + 100.0 + 74.8 = 494.8 \text{ m}$$

F. Why is it important to use vector analysis for this solution?

Answers will vary, but should include that vector analysis is an optimum way to graphically display the location of the instruments and their positions in respect to the airlock.



Scoring Guide

Suggested 15 points total to be given.

Question	Distribution of points
A <i>7 points</i>	1 point for a reasonable sketch 3 points (1 point each) for using the correct equations to find x & y components of the distance for each leg of the trip 3 points (1 point each) for using correct vector addition process to find final displacement for each leg of the trip (step 3)
B <i>3 points</i>	1 point each for correct conversion to vector notation for the three instrument locations
C <i>2 points</i>	1 point for the correct use of the distance formula to determine distance the astronaut traveled 1 point for the correct use of the inverse tangent function to determine the location of the astronaut
D <i>1 point</i>	1 point for the correct use of the distance formula
E <i>1 point</i>	1 point for the correct procedure used to find total distance
F <i>1 point</i>	1 point for reasonable justification

Contributors

This problem was developed by the Human Research Program Education and Outreach (HRPEO) team with the help of NASA subject matter experts and high school AP Physics instructors.

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